

AN ANALYSIS REVIEW: OPTIMAL TRAJECTORY FOR 6-DOF-BASED INTELLIGENT CONTROLLER IN BIOMEDICAL APPLICATION

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ABSTRACT

With advances in automation and robot technology, robots have begun to be widely used in industrial, agricultural, and medical fields, among many other fields. Optimizing the path planning of robot manipulators is one of the core areas of robot research, and it has great research prospects. The precise robot manipulator tracks can improve the efficiency of various robot tasks, such as workshop operations, crop collection, medical surgery and so on. Robot manipulator trajectory planning is one of the core robot technologies, and the design of controllers can improve the trajectory accuracy of manipulators. However, most controllers designed at this point could not effectively solve the nonlinearity and uncertainty problems of high-degree freedom manipulators to overcome these problems and improve track performance for high degree of freedom manipulators. Developing practical path planning algorithms to efficiently complete robot functions in autonomous robotics is critical. In addition, designing a collision-free path in conjunction with the physical limitations of the robot is a very challenging challenge due to the complex environment surrounding the dynamics and kinetics of robots with different degrees of freedom (DoF) and/or multiple arms. The advantages and disadvantages of current robot motion planning methods, incompleteness, scalability, safety, stability, smoothness, accuracy, optimization, and efficiency are examined in this paper.

Keywords: Bio-mechatronics systems Biomedical Robotics, 6-Degree of Freedom (6DoF), Optimal Trajectory Planning

1. INTRODUCTION

For more than three decades, researchers have been studying bio-mechatronics systems and applications to solve practical and theoretical obstacles, particularly those provided by the robotic and mechatronic applications in the medical and healthcare sectors. Biomedical robotics and bio-mechatronic research include a wide range of rapidly developing multidisciplinary fields, such as bio-inspired robots for medical, military, industrial, and rehabilitative applications. In addition, designing and developing bio-inspired systems and devices, including innovative and high performance, have been investigated in various applications. This special issue highlights recent advances and the most exciting mechatronic and robotic applications in many fields. It combines various topics that cover several definitions, developments, controls, and bio-mechatronic/robot deployment practices. Including wearable robot systems like exoskeletons, social robots, rehabilitation robots, and telerobots. This special issue aims to examine bio-mechatronic systems that are biological from

a perspective, as well as the engineering and scientific concepts that underpin their exceptional performance. This work covers high-quality original papers with novel concepts and ideas that use bio-mechatronic and biomedical robotic systems. The recent growth of multidisciplinary research will advance bio-mechatronic and biomedical robotic systems and their applications in rehabilitation, personal assistance, prosthetics, assistive technology, surgery, diagnosis, transportation, and health care in hospitals and laboratories [1].

Biomedical robotics and biomechanics employ numerous rapidly expanding transdisciplinary areas, such as biologically inspired robots for medical, defense, industrial, and therapeutic systems. The most recent and fascinating advancements in robotics and mechatronics span a wide range of topics, including control, definition, development, and application of mechatronic/bio-robotic systems including social challenges. Examples of robotics and wearable robot systems include exoskeletons, rehabilitation robots, remote robots, and other systems engineering techniques like control, optimization, and modeling [2]. Robotic arms, like other mechatronic devices, are made and sold on a large scale internationally. Numerous companies offer hundreds of different kinds of weapons, the majority of which are intended to support industrial production and assembly lines. By mounting numerous tools on their standard wrist connectors, these arms are used in various applications requiring high accuracy and repeatability (e.g., welding, manipulation, spraying). Most research on commercially accessible arms is conducted by robotic enterprises and the laboratories that work with them to improve the design/performance of mechanical/control systems [3]. These arms are a necessary product and a low-cost testbed for research models studying intelligent control systems and novel applications due to their dependability and robustness. As a result, choosing an appropriate robot arm and controller for a study becomes crucial from the perspective of the researcher. In addition to the arm's standard parameters, such as the need for a workspace, weight, repeatability, payload, and degrees of freedom (DOF), other factors need to be taken into account. These include the availability of an after-sales service, a software simulator, the capacity to combine old and new software, the flexibility to add new sensing devices, and the controller. To ensure future scalability, it is essential to assess these qualities before making a final purchasing decision.

The need for 6 degrees of freedom stages in precision engineering is significant. These stages must be exact, with a nanometer-level precision (Willson and Roman, 2008). Precision compliant stages with 3, 5, and 6 degrees of freedom have been discovered in the literature. In each of the six DoF phases, there were three degrees of freedom for both translational(x , y , z) and rotational(x , y , z). Every stage in the 3 DoF has one rotational (z) and two translational (x , y) degrees of freedom, while in considering the rotation around the z -axis, there is no degree of freedom for one 5 DoF stage (Wang et al., 2005). In literature, all of the designs were entirely compatible. In another way, no traditional joints were employed to transmit motion. Aside from that, all of the designs were quite symmetrical.

Trajectory planning is moving a robot between two alternative configurations over time to complete a job while staying within the robot's restrictions. For the robot manipulator, a specific configuration involves a set of joint angles, while the collection of every available joint angle represents the space configuration. The physical restrictions of robots are included in the constraints. Geometric restrictions, which may be described in robot joint angles, are among them (i.e., avoiding collision with the environment, bounds on the joint angles) [4]. They also contain higher-order time derivatives of joint angles and kinematics and dynamics restrictions (i.e., motor current inputs, torques, accelerations, or bounds on the joint velocities).

Furthermore, the task must be completed efficiently and precisely across successive configurations while accomplishing a certain objective, such as minimizing jerk, optimizing smoothness, and reducing energy consumption (or actuator effort), path traversing distance, and execution time. For dynamics-based control approaches, parallel robot dynamic models must be accurate [5]. In reality, it is impossible to avoid a conflict between the established dynamic model and the actual system. This error will have a negative impact on the control's performance [6, 7]. Additionally, the parameter values of dynamic parallel robot models are constantly being updated by the robot motions, necessitating expensive calculations and placing greater strain on the processing power of the controllers. In kinematic-based control approaches, the parallel-robot actuators are presumptively self-governing of one another [8]. By adjusting each target tracing trigger, the robot can travel in the direction it is intended to go [9]. The uniaxial motion controller and the kinematic-based control approach have almost identical designs. There is no need to consider a parallel robot-dynamic model as a result. The application of it is easy.

On the other hand, the motors are not independent in practice. They are connected via the CPU, and the moveable manipulator applies constantly changing load pressures to each operator. As a result, the anti-disturbance ability of the uniaxial motion controller has an essential effect on the performance of the kinematic-based control technique.

Much of the current research has been on building more sophisticated robotic systems and degrees of freedom to aid locomotor training for more complex motions, including gait [10] and multi-joint arm and hand movements. They also make gadgets portable in everyday activities [10]. Additionally, progress has been made in establishing control techniques influencing how these gadgets interact with individuals. Control approaches for parallel robots are critical, particularly for direct drive actuators, because uncertain system disturbances directly affect them [9, 10]. Based on kinematics and dynamics, control techniques for parallel robots may be categorized [11, 12].

2. BACKGROUND

As mentioned in the linked works below, multiple distinct optimum trajectories dominate the 6-DOF-based intelligent controller in biomedical applications and other studies:

Two alternative path optimizers are derived using the free-time optimization control method. Using a seven-speed DOF robot, the two resultant algorithms that encode two different game styles are the defensive player and the central player [13]. In dynamic systems, the ANFIS

technique is an application of Artificial Neural Networks (ANN) that prepared for any frame of care by adding a training signal system to the diverse learning base, using a mixture of slope ratios and small square error (LSE) technology. They also employed a 7-DOF controller. [14] The neural network approach was used to navigate a humanoid robot. The parameters are left and right obstacle distances, the front obstacle distance, and the heading angle. The neural network's output is steering angle [15]. Based on the 6-DOF parallel robot kinematics, a control approach regulated six linear motors to trace their respective intended trajectories underneath a developed Fractional Order Active Disturbance Rejection Controller (FOADRC)[16]. The forward kinematic model uses the Denavit Hartenberg (DH) 6 DOF robot arm placement parametric scheme. The applied inverse kinematic model on an actual robot arm, while the forward kinematic model is examined in MATLAB using Robotics Toolbox [17]. The quintic polynomial function is used for each robot joint to fulfil multiple specific points, where mathematical expressions are generated for each common robot variable over time. The optimized adaptive genetic algorithm improves each joint's interval of interval points to achieve the optimum path planning time. [18]. The robot trajectory is updated, and its real-time target with no need for extra offline iterations. Based on control optimization and gradient ratios, it extends to controllers of linear quadratic regulators to circulate locally, or globally controllers modulate the robot's core path [19]. An improved cetacean improvement algorithm (IWOA) based on the algorithm of differential evolution (DE) and the algorithm of whale improvement (WOA) has been proposed [20]. Artificial neural networks and evolutionary algorithms are used to control the lower limb rehabilitation system built on a parallel Stewart 6 DOF robot (smart strategy). [21]. Kinematics creates a six-degree-of-freedom (DOF) arm of the robot and evaluates its working space. The suggested approach allows manipulator control to accomplish any position and direction [22]. Finding an optimum trajectory from a beginning and end location in the operating space for a particular route. Using a genetic algorithm to calculate the optimum trajectory for a 3DoF spherical wrist with a concurrent axis [23]. A novel grid-based technique for robot path rolling planning in an unknown and static environment Ant colony optimization (ACO) coupled with the ecological knowledge of the local view of the robot and target information is used to intelligently design the robot's local navigation optimization path [24]. A novel framework for generating a trajectory for robotic table tennis that does not use a fixed striking plane. Two alternative trajectory optimizers are created using a free-time optimum control approach[25]. A metaheuristic optimization technique for the planning mobile robot path problem. A comparison of ACO and particle swarm algorithms is carried out. [26]. A novel method and test its efficacy in optimal grinding robot trajectory planning. An objective function was created based on jerk and time. The differential evolution algorithm (DE) and the whale optimization algorithm (WOA) are used to develop an improved whale optimization algorithm (IWOA) [29]. Analyzing Particle Swarm Optimization (PSO), Genetic Algorithm (GA), and Ant Colony Optimization (ACO) metaheuristic techniques to select the multicriteria ad hoc network path pairs. As multicriteria, the power consumption, load variation, and signal-to-noise ratio (SNR), are utilized [30]. Adapt a global attraction phrase that directs ants to the goal site. The Ant colony Algorithm is used in several approaches for

robot path planning. [31]. A humanoid's navigational controller has been created utilizing an intelligent algorithm of fuzzy logic to avoid obstacles in the surroundings and securely reach the intended destination point [32]. A neural network approach guided humanoid robots through a crowded environment filled with numerous hazards. In a crowded environment, the "ROBONOVA" humanoid can travel to the target position in a safe mode by employing the neural network approach, as has been discovered [33]. Making the case that physical human interaction is instructive: it provides information about how the robot should perform its function. Formalize learning from these interactions as a dynamical system in which the task objective has hidden state parameters, and physical human interactions are observations about these parameters [34]. Explores applications to energy and power systems, intending to offer a complete overview of the key challenges surrounding utilizing global optimization metaheuristics problems [35]. The algorithm's performance is evaluated and compared to one another to solve the selection of features in biomedicine successfully. In order to evaluate the searchability of the algorithm fairly and precisely, a set of benchmark problems' feature selection is constructed and provided for performance testing [36]. An improved ant colony algorithm was used for developing the capabilities of effective path planning for mobile robots' difficult maps. In the improved ant colony algorithm, the features of the Ant system's MAX-MIN and the A algorithm are combined [37]. The MVA method is a novel meta-heuristic algorithm based on Multiverse Theory that can tackle NP-hard optimization problems such as nonlinear and multi-level programming issues and practical optimization challenges for CPS systems. [38] In path planning, the suggested method is compared to other algorithms. It was subjected to a performance review to achieve the best learning algorithm [39]. Path optimization addresses the route planning challenge for autonomous mobile robots [40]. The cuckoo optimization algorithm in a dynamic environment is suggested as a novel technique for tackling the mobile robot route planning issue [41]. An adaptive robot gripper and a six-degree-of-freedom robot arm are created by the IRAGS [42]. It is a four-link biped system with an actuated hip joint and passive knee joints that walk independently [43]. Developing optimum trajectory planning algorithms for autonomous robots is critical for completing robot jobs efficiently. Polynomial trajectory planning for a 6-DOF robotic arm is described in [44]. Trajectory planning and joint space simulation were carried out based on kinematics analysis. Kinematics of a three-degree-of-freedom robotic manipulator [45]. The Artificial Neural Networks (ANNs), Genetic Algorithms (GAs), and algebraic method function are the methodologies [46]. Besides the basic optimization algorithms such as GA, PSO, and tabu search [47], there is a continual development of novel optimization algorithms (between 2000 and 2020). To investigate the kinematics and dynamics of degree-of-freedom multiple situations of surgical micro-robot, as well as the best trajectory planning [48]. The challenge of planning path algorithms and optimize dynamic and static situations is the focus of mobile robotics research [49]. The method of smooth trajectory planning and the time-optimal is developed and subsequently applied to robot manipulators [50]. Introduces collaborative robots, improving work performance, dependability, and cost [51]. Based on the Online Trajectory Generation (OTG) concept, the suggested trajectory controller provides real-time

trajectory computation and easy communication with various components, such as the path planner, trajectory generator, collision checker, and controller [52]. suggest smooth pathways from the robot trajectories observation by utilizing Differential Evolution with different initialization forms, selection pressure, exploration, and exploitation to optimize fitting and smoothness requirements [53]. Potential functions are used in an improved technique to plan a wheeled mobile manipulator's collision-free trajectory in blocked settings [54]. A flexible snake-like robot design is given, as well as the constraints model provided for kinematics and obstacle avoidance while moving, motion trajectory planning, and dynamics control [55]. A novel potential function-based technique for wheeled mobile manipulators' collision-free trajectory planning in blocked settings [56]. The development of a novel "whip-lashing" approach on the base of the robot arm's motion is comparable to the action of the whip [57]. It proposes and shows a technique for designing smooth path-constrained time optimum manipulator trajectories. These trajectories are produced by minimizing the jerks needed by the intended motion [58]. an effective approach for determining the best robot base location for performing necessary trajectories of end-effector while redundant copy the wrist partitioned 6 R articulated robots [59]. To increase the speed of industrial robots by generating the shortest-time trajectories that fulfil different restrictions typically used in industrial robot applications [60]. A new planning technique of robot route-rolling in unknown and static environments is suggested on the base of grid modelling. For the robot in an unfamiliar scenario, generating an intelligent local navigation optimization path is accomplished by combining (ACO) with the ecological knowledge of the local view of the robot and the information target [62]. A new planning technique of robot route-rolling in an unknown and static environment is suggested on the base of grid modeling.

3. TRAJECTORY PLANNING ANALYSIS

Robot trajectory planning generally refers to tracking points based on assumptions and a goal posture. Later, and then adjusting the rotational angle of each robot connection to the effector's end along a trajectory led by each point to reach its targeted point ultimately. Cartesian space trajectory planning is more suitable and time-consuming than joint space trajectory planning. As a result, numerous fixed locations at the ends of several robotic arms are often provided [64]. The robot's track points are then calculated using inverse kinematics to transform them from Cartesian space to joint-coordinate space. Following that, the track points are utilized to do interpolation using various polynomial, spline functions, or other formulas and curves for each joint variable time of the generated robot. Furthermore, because of the mechanical properties of the robot, each arm's joint acceleration and speed should be confined to the permissible range. As a result, optimizing the arm's joint acceleration and speed is required to ensure smooth functioning of the joint arm and decrease wear and influence on extending the robot's working life[64].

The robotic control system should provide reference inputs to ensure the planned motion is carried out to solve the trajectory planning problem. Typically, the path created by the path planner, the robot's kinematic and dynamic restrictions, are sent into the trajectory planning

algorithm. The trajectory of the end effector or the joints, in the series of location form, data acceleration, and velocity, is the trajectory planning module output [65].

Because the task to be completed and the difficulties to overcome are stated more naturally in the operating over the joint space, the geometric path is generally established in the robot's operational space. As a result, creating a set of values specifying the position and orientation that the robot's end-effector should acquire at each interval is required while planning the route in the operative environment. When motion follows a path with specific geometric properties established in the functional space, the trajectory is usually scheduled in space operation. In this situation, paths can be characterized precisely (by following the original path) or roughly (by assigning specific route points and utilizing polynomial sequences to link them). In most cases, the path is planned in the joint space of the robot because the manipulator's control action is performed on that joint. Planning in the operational space necessitates a kinematic inversion to convert the end-effector's orientation and position information into a common value. Trajectory planning procedures can be pretty different [66]:

- with a pre-defined path
- point to point

Or:

- in the joint space;
- in the workspace,
- Specifying certain places of interest (starting and ending locations, through a set of points) or the entire geometric path $x = x(t)$. Two factors must be specified to plan the desired trajectory:
 - A geometric route
 - A law of motion

with constraints on the path's smoothness (continuity) and time-derivatives up to a recognized degree.

The geometric path's definition is either the joint space or the workspace. It is usually stated in a parameter form like

$$p = p(s) \quad \text{workspace}$$

$$p = p(\sigma) \quad \text{workspace}$$

The law of motion is $s = s(t)$ ($\sigma = (t)$) which is derived once the parameter s (σ) is specified as a time function.

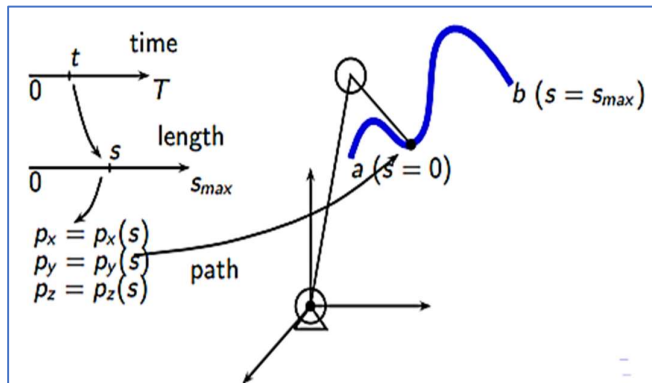


Figure (1) Geometric paths

Parabolic segments, circular, Linear or, more broadly analysis function tracts are examples of geometric pathways (in the workspace). Geometric pathways are created in the joint space by giving the joint variables initial/final (also, in some circumstances, intermediate) values and the desired law motion. In the motion law, continuous functions up to a specific order of derivations are required (often at least first and second order, i.e., acceleration and velocity). Correct degree n polynomial functions are commonly used:

$$s(t) = a_0 + a_1t + a_2t^2 + \dots + a_nt^n$$

These results are in a "smooth" points' interpolation that defines the route geometry.

In most cases, the user has to provide basic information regarding the trajectory, such as the start and stop positions, motion length, maximum velocity, etc.

1. **Workspace trajectories** allow for direct consideration of path constraints (route geometry, obstacles, etc.) in the same space that are more challenging to address (because of the nonlinear kinematics)
2. **Joint space trajectories** are more computationally straightforward and enable concerns like singular configurations, actuation redundancy, and velocity/acceleration limitations.

Specific characteristic points define joint space trajectories, directly allocated by some requirements, defined by describing desired configurations x in the workspace, and then translated into joint space using the inverse kinematic model. The algorithm that evaluates a function $q(t)$ interposes the given points must have important attributes. The paths should be computationally efficient, while the velocity and position patterns should be at least continuous-time functions, and undesirable effects (like non-regular bends) should be reduced or avoided entirely. A single joint is considered in the following discussion. If there are multiple joints, a coordinated motion must be planned, such as considering the same initial and final time instant for each of them, or assessing the joint that are most stressed (with the greatest displacement) and then appropriately scaling the motion of the remaining joints

In most cases, the joint space method is used, and the paths are formed by various interpolation functions, like polynomials.

The polynomials trajectories: In the most specific circumstances, a segment of a path is defined as (period) specifying initial conditions and the final ones for a time, acceleration, velocity, position, and so. The difficulty then becomes determining a function.

$$q = q(t) \text{ or } q = q(\sigma) \quad \sigma = \sigma(t)$$

as a result of which those prerequisites are met. It is a problem of boundary conditions that can be handled quickly by using polynomial functions like:

$$q(t) = a_0 + a_1t + a_2t^2 + \dots + a_nt^n$$

The polynomial's degree n (3, 5...) determines the boundary conditions' number that needs to be confirmed and the required trajectory smoothness.

In addition to the starting and end values, other restrictions might be put on various time derivatives' values (jerk, acceleration, velocity, etc.) in generic instants t_j . In other words, creating a polynomial function $q(t)$ whose k th derivative has a defined values $q^{(k)}(t_j)$ at a specific time, t_j might be of relevance. These requirements can be represented mathematically as:

$$k! a_k + (k + 1)! a_{k+1}t_j + \dots + \frac{n!}{(n - k)!} a_n t_j^{n-k} = q^{(k)}(t_j)$$

or, in matrix form: $M_{a=b}$

Where:

- M is matrix $(n + 1) \times (n + 1)$,
- b is the vector with constraints of $n + 1$ on the path (the data known),
- $a = [a_0, a_1, \dots, a_n]^T$ contains the parameters that unknown in order to be computed

$$a = M^{-1}b$$

- **Third order polynomial paths:** Given an initial instant t_i and a final one t_f a (segment of a) path can be determined by allocating initial conditions and final ones:
 - Initial position q_i , velocity \dot{q}_i
 - Final position q_f and velocity \dot{q}_f

Because there are four boundaries, a polynomial of degree 3 (or higher) should be recognized.

$$q(t) = a_0 + a_1t + a_2t^2 + a_3t^3$$

The four parameters a_0 , a_1 , a_2 , and a_3 must be defined to satisfy the boundary conditions. It follows from the boundary conditions that

$$q(t_i) = a_0 + a_1 t_i + a_2 t_i^2 + a_3 t_i^3 = q_i$$

$$q(t_i) = a_1 + a_2 t_i + a_3 t_i^2 = q_i$$

$$q(t_f) = a_0 + a_1 t_f + a_2 t_f^2 + a_3 t_f^3 = q_f$$

$$q(t_f) = 2a_2 t_f + 3a_3 t_f^2 = q_f$$

Let us assume that $t_i = 0$ for the time being in order to solve these equations. Therefore: Profiles of acceleration, velocity, position obtained to use a cubic polynomial and boundary conditions: $q_i = 100$, $q_f = 300$, $\dot{q}_i = \dot{q}_f = 0$ o/s, $t_i = 0, t_f = 1$ s:

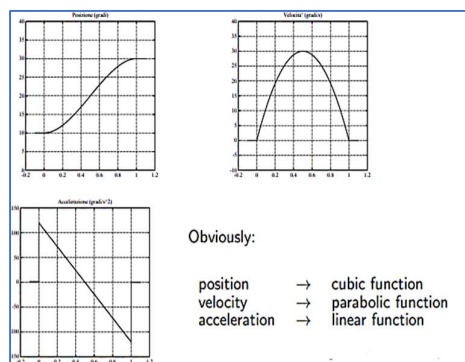


Figure (2) polynomial

The obtained results with both polynomial (1) and the coefficients (3)-(6) are generalizable to the case where $t_i \neq 0$. One receives:

$$q(t) = a_0 + a_1(t - t_i) + a_2(t - t_i)^2 + a_3(t - t_i)^3 \quad t_i \leq t \leq t_f$$

With coefficients

$$a_0 = q_i$$

$$a_1 = q_i$$

$$a_2 = \frac{-3(q_i - q_f) - (2q_i - q_f)(t_f - t_i)}{(t_f - t_i)^2}$$

$$a_3 = \frac{-2(q_i - q_f) - (2q_i - q_f)(t_f - t_i)}{(t_f - t_i)^3}$$

It is simple to plan a trajectory that passes through a series of intermediate points. Profiles of position, velocity, and acceleration with:

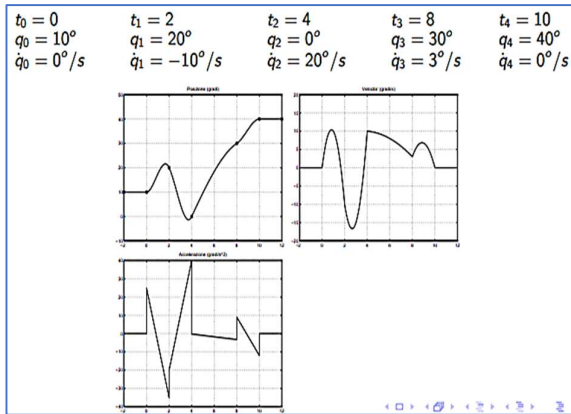


Figure (3) polynomial of six boundaries

- **Fifth-order polynomial trajectories:** profiles of location and velocity are continuous-time functions, as seen. It is not the case with acceleration, which results in discontinuities between segments. Furthermore, giving appropriate initial/final values for this signal in each segment is impossible. These features are not a concern in many applications because the trajectories are "smooth" enough. If, on the other hand, initial and final acceleration values are required (for example, to obtain acceleration profiles), then fifth-order polynomial functions must be considered (at least).

$$q(t) = a_0 + a_1t + a_2t^2 + a_3t^3 + a_4t^4 + a_5t^5$$

With conditions of six boundaries:

$$q(t_i) = q_i \quad q(t_f) = q_f$$

$$\dot{q}(t_i) = \dot{q}_i \quad \dot{q}(t_f) = \dot{q}_f$$

$$\ddot{q}(t_i) = \ddot{q}_i \quad \ddot{q}(t_f) = \ddot{q}_f$$

In this situation (if $T = t_f - t_i$), the polynomial coefficients are

$$a_0 = q_i$$

$$a_1 = \dot{q}_i$$

$$a_2 = \frac{1}{2} \ddot{q}_i$$

$$a_3 = \frac{1}{2T^3} [20(q_f - q_i) - (8\dot{q}_f - 12\dot{q}_i)T - (3\ddot{q}_f - \ddot{q}_i)T^2]$$

$$a_4 = \frac{1}{2T^4} [30(q_f - q_i) - (14\dot{q}_f - 16\dot{q}_i)T - (3\ddot{q}_f - 2\ddot{q}_i)T^2]$$

$$a_5 = \frac{1}{2T^5} [12(q_f - q_i) - 6(\dot{q}_f - \dot{q}_i)T - (\ddot{q}_f - \ddot{q}_i)T^2]$$

If a set of points is provided, the intermediate velocity values can be computed using the same considerations as for third-order polynomial trajectories. Polynomial trajectories are a type of polynomial trajectory. The following is a fifth-order trajectory with boundary conditions:

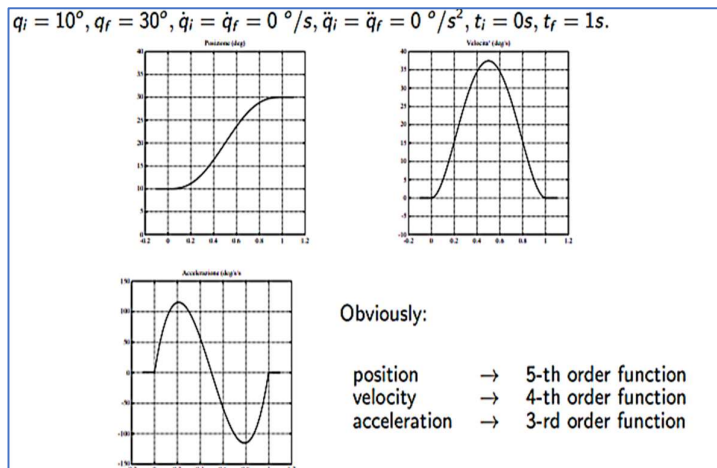


Figure (4) polynomial of four boundaries

3.1 . Classic Approaches

Creating a geometric path without a temporal law is what trajectory planning entails, whereas trajectory planning involves giving the geometric path a time law. Off-line and online are two algorithms of trajectory planning classified depending on the information provided. Offline robots could calculate the target's path before motion occurs when the environment is completely known (i.e., information about obstacles is known from the beginning), resulting in a globally optimum solution. This category covers a wide range of topics. The topics include optimality (locally and globally) and completeness. The solution will be discovered if one exists. Moreover, cost and computational efficiency (permit changings without replanning or recomputing everything). Online robots progressively develop the route to the goal during mobility, resulting in local optimum solutions at their finest. In this case, the mobile robot gathers data from sensors across the environment. This category includes issues such as

completeness (is the robot guaranteed to reach the aim if a solution is possible), computational efficiency and costs at each level, and optimality (how far is a solution from the optimal, and is it limited by an upper bound). Trajectory planning can be done in a variety of ways. The most important classical methodologies are sampling-based, potential field methods, combinatorial approaches, and bug-like algorithms. The earliest and most fundamental sensor-based algorithms are bug-like algorithms [66]. The robot is believed to be a perfectly positioned point in space with a restricted workspace. They are equipped with a contact sensor that detects the obstacle boundary when it comes into contact with it. They are simple to execute because they must move towards the objective unless an obstacle is met. In that situation, they navigate around the obstruction until a movement toward the goal is once again permitted. It can be done by calculating the distance between two places. Most offline robots employ combinatorial approaches; space configuration as the basic notion is used by geometric representation planners. Geometric representations of the environment might take the form of graphs or roadmaps that encapsulates the open space topology and are constructed using many well known approaches like a visibility graph ([69], [70], [71], [72]), the Voronoi diagram ([67], [68]); a tangent graph [73]; the Subgoal Network [23], Silhouette [82], and cell decomposition and grid method ([74], [75], [76], [77], [78], [79], [80], [81]). They portray free space (non-collision space) differently, but they are all based on a linked network of path segments that can be traced from start to finish. The key computational effort in these approaches is the representation of free space, which includes obstacle mapping. Traditional graph search techniques such as Dijkstra's search [83] or A* [84] are used to identify the shortest path after the roadmap has been created. The advantage of these strategies is that they make the broad motion planning problem NP-complete. However, they have the drawbacks of being too sluggish for practical usage, particularly in high-dimensional issues, and requiring an explicit description of obstacles, which is difficult to get in most actual problems. Another technique is to characterize the search space as an undirected graph[2] using a uniform grid. These approaches impose high costs on edges that cross barriers, allowing nodes in the free space to be effectively separated from inaccessible nodes. The resolution of this method is full, as it is for all systems based on a discrete representation of the search space, which implies how at low grid resolutions, pathways that traverse through tight spaces between obstacles can be ignored. An increase in graph resolution, on the other hand, would result in a significant increase in computational effort. The uniform grid representation has a substantially higher number of nodes than the roadmap-based techniques, which is a drawback. However, this method can be used when impediments are not defined well, like with a mobile robot. The method of potential field creates a high-potential field near the barriers and a low-potential field near the configurable goal ([1], [26]). By allowing the robot configuration to evolve in that potential field, the robot is steered to the aim configuration while averting impediments. In other words, although the obstacles repel the robot, it is drawn to the appropriate configuration. The gradient is a vector that points in the direction of the current location. In contrast, to previous algorithms, sampling-based planners accept probabilistic completeness (i.e., the goal may not be reached in a finite amount of time). They accept any solution (not

necessarily the best) and ignore the explicit geometric representation of the free configuration space in terms of roadmaps or graphs. A roadmap is a graph connecting vertices representing free-space configurations with a path running through the free space. The roadmap can be created in two ways: deterministic or probabilistic. In the Probabilistic Roadmap Planner, samples are chosen randomly in free space rather than following a regular grid (PRM). There are numerous approaches for selecting the pairs of vertices to connect due to the lack of a prior grid structure. This method is effective for a wide range of issues ([27], [28]). It is based on the notion that it is less computationally expensive to see if there is a single robot arrangement in the free space. PRM generates a roadmap in free space by sampling the nodes and edges of the roadmaps with coarse and fine sampling, respectively (i.e., the free trajectory between the configuration of the node). Then, by connecting the target configurations and the initial roadmap, queries about planning could be answered. A uniform random distribution ensures the planner's probabilistic completeness [29]. Other planners that are sample-based and use the nodes sampling method include the planner Rapidly Exploring Random Tree (RRT) [24] and the planner Expansive Spaces Tree (EST) [30], which may be more successful for single-query planning.

3.2 Heuristic Approaches

Metaheuristic and heuristic techniques have been developed to address the shortcomings above of traditional approaches. Probabilistic Roadmaps (PR) methods are included. Rapid exploration of Random Trees (RRT) contains the following:

Ant Colony Optimization (ACO) uses ants' foraging behavior to find the shortest food source path ([32], [33], [34]). Genetic Algorithms (GA) that are based on selection and natural genetics mechanisms ([38], [39], [40]), Simulated Annealing (SA), which is the approach of heuristic random search that mimics the annealing processes for cooling molten metal ([35], [36]) and Neural Network [37]. More techniques include Particle Swarm Optimization (PSO) is inspired by the social behavior of bird flocking or fish schooling for more straightforward implementation using fewer adjusted parameters, as compared to the GA technique ([41], [42], [43], [44], [45], [46]). Also, Wavelet is based on the theory of wave-like oscillations [48]. Fuzzy logic is many-valued logic wherein the variables' truth values might range from 0 to 1 [49]. Finally, Tabu Search is a mathematical optimization method based on local search [36]. Heuristic algorithms do not promise that a solution can be found, but if they want to, they will do it far more quickly than deterministic methods.

3.3 Decision-making process technique for path planning

There are numerous ways to estimate the path of a moving item when accurate knowledge about the robot's environment and geometric description is unavailable. The environment's knowledge is derived from the provided measurements by a set of imprecise sensors, which are noisy in such instances. As a result, trajectory planning is done in the face of uncertainty, which must be predicted. This uncertainty impacts the robot's and its environment's predictability of present states and the states in the future (in continuous or discrete state spaces

and continuous time). These states are determined by the memory of activities that were previously performed, sensors, and initial conditions. As a result, under uncertainty, trajectory planning approaches include problems like manipulation, map creation, pursuit-evasion, and localization [2]. To a greater or lesser extent, some strategies can account for the decision-making process and uncertainty. For example, more advanced methods involve sequential decision-making (a sequence of fundamental problems of decision making), artificial intelligence, and control theory. Probabilistic models, expected-case, or Worst-case, analyses of game theory (with players of competitive objectives. Instead of using a deterministic location, probabilistic estimate methods use the robot's location probability density function (PDF) over space, which allows for coping with uncertainty. The goal is to maintain a PDF position for every robot's potential stance. The Kalman filter [50] is an efficient example of a recursive algorithm to estimate the state of a noisy dynamical system. This is accomplished using Bayesian inference and calculating a joint probability distribution over the variables for each period. It generates a Gaussian probability density function (PDF) of potential robot positions instead of a single position estimate, with the mean and covariance of the error covariance matrix acting as a distribution. Another method for tracking mobile robots in dynamic environments is the Markov process, often known as the Markov decision process (MDP). When outcomes are partially unpredictable and partly under the control of a decision-maker, it employs a probabilistic framework for decision-making. It has the advantage of providing an optimal path, but it has the drawback of restricting the robot's possibilities to a small number of them. As a result, the path was not smooth. Although, Fuzzy Markov decision processes (FMDPs) can yield smooth trajectories [51]. The Kalman filter employs the same iterative prediction-update procedure as Bayesian approaches, but it does not depend on the restrictive assumptions of Kalman filter [52]. The advantages include using nonlinear models for both sensing and arbitrary distribution and path planning rather than a Gaussian. However, this could result in a more computing cost than Kalman filters.

3.4 Mathematical programming

Mathematical programming-based obstacle avoidance systems apply a set of inequalities to the configuration parameters. Motion planning is then introduced as a mathematic problem optimization in which the goal is to identify the curve between the beginning and the goal configurations that minimize or maximize a particular goal function. For instance, energy consumption (or actuator effort), execution time, path traveling distance, and jerk, or maximizing smoothness (e.g., [53], [54], [55]). It creates a nonlinear problem optimization with multiple inequalities and differential constraints that must be addressed numerically. Furthermore, Pareto optimum solutions have been developed in the literature for multi-objective optimization issues ([56], [57]).

3.5 Approaches Comparison

The advantages and disadvantages of the various techniques are shown in table 1. Completeness (whereas if the path is available, the path and trajectory are found). Optimality (the acquired plan is optimal in terms of specific parameters, not stuck in a local minimum).

Efficiency (the computational cost of the algorithm, i.e., if it can change the queries and the world without repeating computing everything or re - planning from the start) are among the issues that have been addressed. Additional challenges include execution time (lower times are desirable), accuracy (high precision path tracking and controversies) (for the robot, its surroundings, and humans), and scalability (the problem grows effectively as the configuration space dimensions significantly rise). On the other hand, robot trajectory planning optimization approaches are continually evolving (e.g., [59], [60], [61]).

Table 1. Summary

Approach	Pros	Cons
Potential fields	Real-time, good scalability	Not complete, not efficient world and queries update>, path not optimal (local minimum), potential field forces must be set
Cell decomposition	Complete,	High computational cost, and high execution time
Visibility graph	Complete and yields minimum length paths, optimal	High computational cost, and high execution time, bad scalability, not efficient world and!Ue ries undates
Voronoi diagram	Complete and generates roadmap with maximum distance, efficient worldandaue.ries uodates	Possibly inefficient paths, time, bad scalability, path not ootima
Heuristic approaches	Low execution time, parallel Search	Not complete, the possibility of providing smooth oaths
Exact cell decomposition	Complete	High computational cost, high execution time
Approximate cell decomposition	Robust and useful when only a coarse representation of the workspace is available	Not complete
Bug (bug 1 and bug 2)	Complete, easy implementation, parameters eas:v to adiu\$f:	Long paths, high execution time

A*	Complete, optimal grid	Not efficient , bad scalability, not efficient world updates
Rapidly exploring random tree (RRT)	Complete, semi-efficient world and queries updates, good scalability	Path not optimal
Probabilistic roadmap (PRLvs)	Complete, semi-efficient queries updates, optimal graph, good scalability	Not efficient world updates

1. System Modeling of 6-DOF Robot

The robotic arm with 6 degrees of freedom robotic platform employed in this study is the ED7220C, which ED Korean Corporation built. The robot arm has been used widely in research, education, and development. It is essentially a series that manipulate all joints arranged in a revolution shape. As illustrated in Figure (4), the arm geometry consists of the elbow, shoulder, waist, and wrist by the human arm joints.

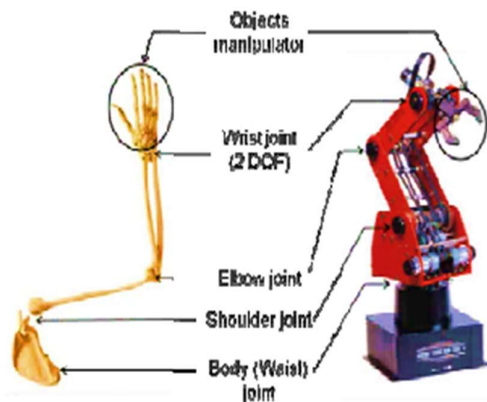


Figure (4) 6 Degree of Free

Because the wrist may move the two planes (pitch and roll), the end effector is more versatile in object handling.

The robot, which is built with vertical articulation, allows for the quick visual study of each joint of mechanical behavior. A micro-servo motor drives the entire arm, with each DOF achieved via an optical encoder (DME 38B50G). A dual-state clutch with rubber pads serves as the last transponder.

In a control algorithm malfunction, built-in mechanical safety restrictions prevent joint movement. The key features of the ED7220C robotic arm are listed in Table 2.

Table 2 ED7220C robotic arm

Feature	Description
Position precision	$\pm 0.5\text{mm}$ (approx.)
Movement speed	100mmfs (max.)
Load capacity	1 Kg
Weight	33 Kg
Wrist Pitch	260°
Ro11	360°
Range Of Motion (ROM)	
Elbow	172°
Shoulder	90°
Waist	360°

The general setup of the robot is depicted in the diagram below, with its control unit connected to a regular computer and an educational pendant. The controller function (ED) provides ports for the encoded motors, allowing the robot to be driven visually. The controller has over 100 cores with higher-level commands, allowing the platform to be used in various ways. The teaching pendant allows the controller to control any of the two. The necklace serves as a driving practice pad. A robotic arm is controlled manually. It is used to allow the robot to recognize any accessible coordinates. The control unit can save the points taught to perform a restart later. On the other hand, the robot must be educated each time the thing's location changes. In order to achieve this, the robotic arm is self-contained. [9] built and presented a robotic image-guided system.



Figure (5) General System of The Robot

- **A. Forward Kinematic Model**

Different methods can be used to investigate a robot's kinematic problem. Denavit-Hartenberg (DH) parameters are employed in two regularly used ways. Both methods are better suitable for simulating serial manipulators since they are methodical. Some researchers also regularly use geometric approaches for serial manipulators with elementary geometry. Because

of its adaptability and suitability for simulating any number of serial manipulator joints and linkages, regardless of complication, the DH technique was utilized to construct the robot's kinematic model in this study. Figure (6) depicts a simplified kinematic model of the robotic arm in an inverted 'L' position. The first three joints move the tooltip to the desired position, while the last two joints change the orientation of the end lengths in Table (3).

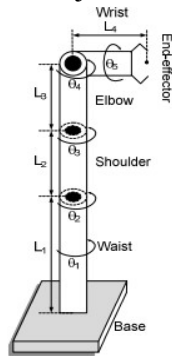


Figure (6) simplified kinematic model of the robotic arm

Table (3) Two joints change the orientation of the end lengths

Joint	Waist	Shoulder	Elbow	Wrist
Symbol	L_1			
Link Length [mm]	385	220	220	155

Link offset, link length, twist angle, and joint angle is all represented by quadruple d, a, α, θ , in DH. As illustrated in Figure (7), the system of an orthonormal coordinate coupled with each manipulator link by DH standard. Table (4) lists the DH parameters for the robotic arm ED7220C.

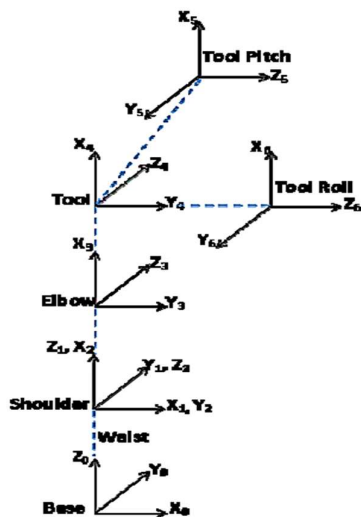


Figure (7) DH parameters for the robotic arm ED7220C.

Table (4) lists the DH parameters for the robotic arm ED7220C.

SYMBLE	1	2	3	4	5	6
$a_i - 1$	0	-90	0	0	-90	0
$a_i - 1$	0	0	L ₂	L ₃	0	0
d_i	L ₁	0	0	0	0	L ₄
θ_i	θ_i	$\theta_2 - 90$	θ_3			0

The corresponding transformation matrices for each link of the robotic arm have been generated using the general form of the transformation matrix for each link (expressing joint I in its preceding nearby joint i-1) derived in [11]. These different transformation matrices, when multiplied, provide the overall matrix reflecting the base's end terms, thanks to the compound transformation property (1).

$${}^0T_6 = \begin{bmatrix} C_1 C_5 S_{234} + S_1 S_5 & -C_1 S_{234} S_5 + S_1 C_5 & C_1 C_{234} & C_1 A \\ -S_1 C_5 S_{234} - C_1 S_5 & S_1 C_{234} C_5 + C_1 C_5 & S_1 C_{234} & S_1 A \\ C_{234} C_5 & -C_{234} S_5 & -S_{234} & B \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (1)$$

Where

$$A = L_2 S_2 + L_3 S_{23} + L_4 C_{234}$$

$$B = L_1 + L_2 C_2 + L_3 C_{23} - L_4 S_{234}$$

The rotation is represented by the 3X3 matrix, which consists of the first three rows and first three columns, while the location (x, y, z) of the base's end-effector was represented in the last column.

• Inverse Kinematic Model

The inverse kinematic (IK) model has greater applicability in real-world robotic systems. IK is important not only in robotics but also in other industries, such as 3D games. IK, unlike forwarding kinematics, there is not a single solution to it. The systems that guarantee free of collision operation and joint with minimal motion are the best. The IK model of ED7220C was developed using an analytical technique. This method ensures that the model determines joint angles correctness for any object within the workspace of the robotic arm. The joint angles required to accomplish the specified position and orientation are computed using the IK model. The mechanical arm movement control and planning are based on inverse kinematic robotics analysis. The known end-effector, related to the reference coordinate system's position and linkage parameters, determines the value of each joint angle i. This method is used to calculate the first four joint angles: waist (_1), shoulder (_2), elbow (_3), and toll pitch (_4), whereas tool roll (_5) is directly determined by the desired orientation for object manipulation.

Because rotation and translation are involved in transformation, the usual form of the transformation matrix from tool to base is ()

$${}_{Tool}^{Base}T = \begin{bmatrix} n_x & o_x & a_x & p_x \\ n_y & o_y & a_y & p_y \\ n_z & o_z & a_z & p_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

In an IK problem, the first 3x3 matrix and (px, py, and pz) indicate the translation and rotation of the end-effector w.r.t the base of the robot. After extensive mathematical computations, the established analytical IK model offers equations (), (), (), and () for the joint angles θ_1 , θ_2 , θ_3 , and θ_4 , respectively. The requisite joint angles are expressed as coefficients in these equations ().

$$T1 - 1 * T = T2 * T3 * T4 * T5 * T6$$

$$\theta_1 = \text{atan2}(d, py, px)$$

$$d = \text{sqr}(px^2 + py^2)$$

$$r_4 = d - a_4 * \text{Cosd}(\theta_{234})$$

$$z_4 = p_z - a_4 * \text{Sind}(\theta_{234})$$

$$\theta_3 = \text{acosd}\left(\frac{z^2 - a_2^2 - a_3^2}{2 * a_2 * a_3}\right)$$

$$\text{beta} = \text{atan2}(a_3 * \text{sind}(\theta_3), a_2 + a_3 * \text{cosd}(\theta_3))$$

$$\text{alpha} = \text{atan2}(z_4 - a_1, r_4)$$

$$\theta_2 = \text{alpha} + \text{beta}$$

$$\theta_4 = \theta_{234} - \theta_3 - \theta_2$$

$$\theta_5 = \text{acosd}\left(\frac{\text{sind}(\theta_1) * px - \text{cosd}(\theta_1) * py}{\text{sind}(\theta_4) * a_5}\right)$$

$$\theta_6 = \text{atand}\left(\text{cosd}(\theta_5) * \text{cosd}(\theta_4) * \text{sind}(\theta_2 + \theta_3) + \text{sind}(\theta_5) * \text{cosd}(\theta_2 + \theta_3) - \text{sind}(\theta_4) * \frac{\text{cosd}(\theta_5)}{\text{cosd}(\theta_5) + \text{sind}(\theta_4) + \text{sind}(\theta_2 + \theta_3)}\right)$$

• IK Model Implementation

The IK model has been implemented on the arm manipulator of the genuine robot. A known position and orientation have been assigned to an object. The created method initially evaluates if the object is inside the robot workspace using this known information from the user, as shown in IK. The algorithm finishes after prompting the user if the object is not inside the scope of the work. Otherwise, the IK model calculates the necessary joint angles for the end-effector to point in the correct position and orientation. The low-level encoder ticks are then transferred to these joint angles. Finally, the program's Kernel-based instructions carry out the commands for moving the robotic motors according to the mapped encoder ticks. The figure illustrates the flow chart implementation of the model.

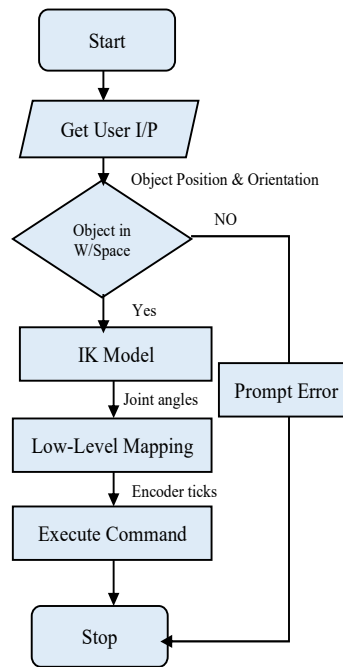


Figure (8) PH implementation of the model

To execute the generated IK model on the robotic arm, the object (for example, a vehicle key with a key) must be within the robotic arm workspace. For this purpose, two blocks are used to raise the platform on which the object is put (in height z). The task at hand is shifting an object from one area to another. The position and orientation of both the source and destination have been provided as inputs. The robot moves according to computed joint angles based on the user's object coordinates (IK model). The gripper shuts when the robot reaches the target spot, and the object is grasped. Picking up the thing in order, The robot moves using the coordinates the user has also taught it. The point of the target must be inside the operational workspace of the robot. After arriving at that location, the robot drops it and returns to its original station.

6. CONCLUSION

This study gives an overview of the best autonomous robot trajectory planning methods. They address a wide variety of topics, including robot kinematics, achieving collision-free trajectories, and taking the robots' physical constraints into account. The various motion planning approaches are reviewed and their benefits and drawbacks. As a result of these advantages and disadvantages, various methods may be employed for a wide range of robot applications.

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